

Seismic Analysis of a Reinforced Concrete Building by Response Spectrum Method

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Abstract: - Seismic analysis of a multi-story RC frame in Khartoum city was analyzed under moderate earthquake loads as an application of seismic hazard, and in accordance with the seismic provisions proposed for Sudan [1] to investigate the performance of existing buildings if exposed to seismic loads. The frame was analyzed using the response spectrum method to calculate the seismic displacements and stresses. The results obtained, clearly, show that the nodal displacements caused drifts in excess of approximately 2 to 3 times the allowable drifts. The horizontal motion has a greater effect on the axial compression loads of the exterior columns compared to the interior columns and the compressive stresses in ground floor columns were about 1.2 to 2 times the tensile stresses. The values of shear forces due to L/C3 in beams B805, B806 and B807 were found to be about four times the values due to L/C1. The maximum values of compressive and tensile stresses in beams are approximately equal. Bending moments in beams and columns due to seismic excitation showed much larger values compared to that due to static loads.

Keywords: - Displacements, Drifts, Seismic Analysis, Seismic Hazard, Stresses, Sudan

I. INTRODUCTION

Earthquakes, caused by movements on the earth surface, result in different levels of ground shaking leading to damage and collapse of buildings and civil infra-structures, landslides in the case of loose slopes, and liquefaction of sandy soil [2]. The behavior of reinforced concrete moment resisting frame structures in recent earthquakes all over the world has highlighted the consequences of poor performance of beam column joints [3]. Beam column joints in a reinforced concrete moment resisting frame are crucial zones for transfer of loads effectively between the connecting elements (i.e., beams and columns) in the structures [3]. Traditionally, seismic design approaches are stated, as the structure should be able to ensure the minor and frequent shaking intensity without sustaining any damage, thus leaving the structure serviceable after the event [4]. The structure should withstand moderate level of earthquake ground motion without structural damage, but possibly with some structural as well as non-structural damage. This limit state may correspond to earthquake intensity equal to the strongest either experienced or forecast at the site. The results are studied for response spectrum method. The main aim of this paper is to investigate the seismic performance of a reinforced concrete moment resisting frame building under a moderate earthquake ground motion. The building, which is located in Khartoum City (zone 2), was analyzed in accordance with the suggested seismic provisions proposed for Sudan [1].

II. RESPONSE SPECTRUM METHOD

The response spectrum represents an envelope of upper bound responses, based on several different ground motion records. This method is an elastic dynamic analysis approach that relies on the assumption that dynamic response of the structure may be found by considering the independent response of each natural mode of vibration and then combining the response of each in some way. This is advantageous in the fact that generally only few of the lowest modes of vibration have significance while calculating moments, shear and deflections at different levels of the building.

Following procedure is generally used for the spectrum analysis [2]:

- [1] Select the design spectrum.
- [2] Determine the mode shapes and periods of vibration to be included in the analysis.
- [3] Read the level of response from the spectrum for the period of each of the modes considered
- [4] Calculate participation of each mode corresponding to the single-degree-of-freedom response read from the curve.
- [5] Add the effect of modes to obtain combined maximum response.
- [6] Convert the combined maximum response into shears and moments for use in design of the structure.

III. RESPONSE SPECTRUM METHMOD BY USING STAADPRO

This is accurate method of analysis. The design lateral force at each floor in each mode is computed by STAADPro [5]. The software provides results for design values, modal masses and storey base shear. STAAD utilizes the following procedure to generate the lateral seismic loads.

- [1] Program calculates time periods for first six modes or as specified by the user.
- [2] Program calculates Sa/g for each mode utilizing time period and damping for each mode.
- [3] The program calculates design horizontal acceleration spectrum Ak for different modes.
- [4] The program then calculates mode participation factor for different modes.
- [5] The peak lateral seismic force at each floor in each mode is calculated.
- [6] All response quantities for each mode are calculated.
- [7] The peak response quantities are then combined as per method (CQC or SRSS or ABS or TEN or CSM) as defined by the user to get the final results.

IV. LOAD COMBINATION

In designing for seismic forces, the following two combinations can be considered [1]:

$$A = D + L.p + E \quad (1)$$

$$A = 0.85D + E \quad (2)$$

Where

D = dead load;

L = live load;

P = incidence factor for live load; and

E = earthquake load.

V. FRAME DETAILS AND STUDY CASE

A traditional residential ten-storey regular reinforced concrete frame building located in Khartoum City, with 12 m × 20 m plan as shown in Fig. 1, was analyzed to investigate its seismic performance. The most important parameters governing the analysis of this frame were dead load, live load and seismic loads. Seismic loads were computed based on the Response Spectrum Approach (RSA). Three combinations of load cases were applied as follows:

Load Case 1 (L/C1) is static load (dead and live) are follow the rules given in the (BS 8110, 1997) [6].

Load Case 2 (L/C2) is seismic loads.

Load Case 3 (L/C3) is (static + seismic) loads.

A uniformly distributed gravity load of 20 kN/ m was applied including the own weights of members.

The sections of columns and beams of the frame are shown in Table 1.

Table 1: Sections of Columns and Beams of the frame Building

<i>Floor Level</i>	<i>G - 5th</i>	<i>6th to 7th</i>	<i>8th to Roof</i>
Columns (mm)	500X300	400X300	300X300
Typical Beams (mm)	400X300		

One selected frame (the critical one) was analyzed using STAAD PRO (2006) program. The same ground accelerations versus time periods used in seismic hazard analysis of Sudan [1] were adopted in this paper as input data to calculate the seismic response spectrum parameters, i.e., displacements and stresses. The damping ratio was taken as 0.05 (5% of the critical damping) and typical slab thickness was 130 mm.

Some members of the frame building were selected for the purposes of the analysis. The selected members, which are shown in Fig. (2) were:

Columns: C801, C802, C856, C857, C889 and C890.

Beams: B805, B806 and B807.

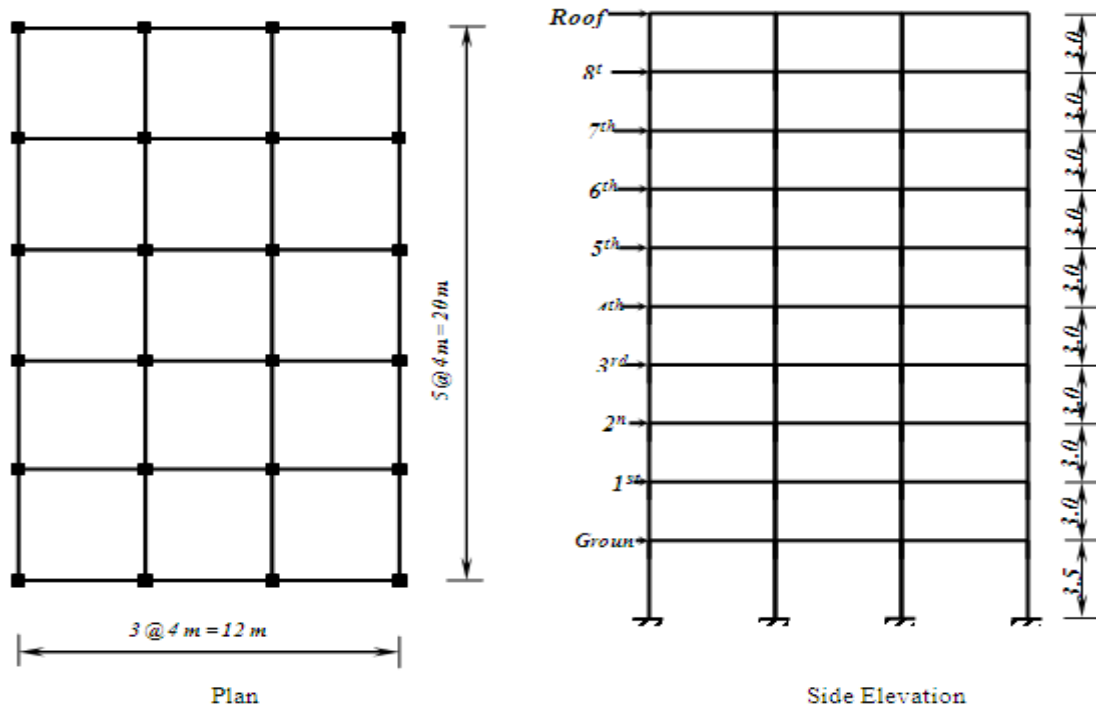


Fig. 1: Dimensions of the Studied Frame Building

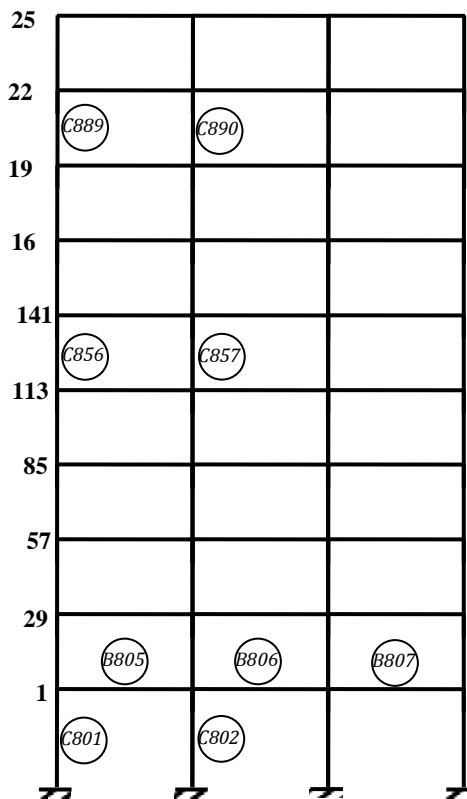


Fig. 2: Selected Nodes and Members of the Studied Frame

VI. RESULTS OF THE ANALYSIS

The analysis was performed for static and seismic loads. The Seismic analysis used horizontal input motion of earthquake with moderate horizontal peak ground acceleration (PGAH). A total time of vibration of 8 seconds was considered. The results of the analysis are shown in Tables 2 to 7 and Figures 3 to 7 as follows:

Table 2: Nodal Displacements of the Studied Frame

<i>Node</i>	<i>L/C</i>	<i>Horizontal X (mm)</i>	<i>Vertical Y (mm)</i>	<i>Horizontal Z (mm)</i>	<i>Resultant (mm)</i>
1	1. Dead+Live	-0.001	-0.270	0.029	0.271
	2. Seismic Loads	20.451	1.381	0.023	20.498
	3. Static+seismic	20.450	1.111	0.052	20.480
29	1. Dead+Live	-0.000	-0.513	0.118	0.526
	2. Seismic Loads	54.201	2.579	0.012	54.263
	3. Static+seismic	54.201	2.066	0.130	54.241
57	1. Dead+Live	-0.000	-0.728	0.257	0.772
	2. Seismic Loads	89.491	3.568	0.014	89.562
	3. Static+seismic	89.490	2.840	0.271	89.536
85	1. Dead+Live	-0.000	-0.915	0.441	1.016
	2. Seismic Loads	123.527	4.355	0.020	123.604
	3. Static+seismic	123.526	3.440	0.461	123.575
113	1. Dead+Live	0.001	-1.073	0.664	1.262
	2. Seismic Loads	155.362	4.955	0.013	155.441
	3. Static+seismic	155.363	3.882	0.677	155.413
141	1. Dead+Live	-0.001	-1.235	0.926	1.544
	2. Seismic Loads	189.988	5.490	0.027	190.067
	3. Static+seismic	189.987	4.255	0.953	190.037
169	1. Dead+Live	-0.000	-1.362	1.222	1.830
	2. Seismic Loads	219.763	5.839	0.029	219.841
	3. Static+seismic	219.762	4.477	1.251	219.811
197	1. Dead+Live	0.002	-1.454	1.546	2.122
	2. Seismic Loads	243.991	6.040	0.024	244.066
	3. Static+seismic	243.994	4.586	1.570	244.042
225	1. Dead+Live	-0.001	-1.532	1.893	2.436
	2. Seismic Loads	269.211	6.157	0.038	269.282
	3. Static+seismic	269.210	4.625	1.932	269.256
253	1. Dead+Live	0.004	-1.567	0.037	2.759
	2. Seismic Loads	283.889	6.185	2.270	283.956
	3. Static+seismic	283.893	4.618	2.307	283.940

Table 3: Storey Drifts in the Studied Frame

<i>Node</i>	<i>L/C</i>	<i>Displacement Resultants (mm)</i>	<i>Drift (mm)</i>
1	Static+seismic	20.48	-
29	Static+seismic	54.241	33.761
57	Static+seismic	89.536	35.295
85	Static+seismic	123.575	34.039
113	Static+seismic	155.413	31.838
141	Static+seismic	190.037	34.624
169	Static+seismic	219.811	29.774
197	Static+seismic	244.042	24.231
225	Static+seismic	269.256	25.214
253	Static+seismic	283.94	14.684

Table 4: Column End Forces of the Studied Frame

<i>Column</i>	<i>L/C</i>	<i>Node</i>	<i>F_x</i> (kN)	<i>F_y</i> (kN)	<i>M_z</i> (kN.m)
C801	1. Dead+Live	281	748.451	-7.11	-6.94
		1	-737.651	7.11	-14.394
	2.Seismic Loads	281	1726.257	246.283	591.915
		1	-1726.26	-246.283	-146.98
	3.Static+seismic	281	2474.708	239.172	584.976
		1	988.607	253.394	132.586
C802	1. Dead+Live	282	1202.8	-0.29	-0.31
		2	-1192	0.29	-0.561
	2.SeismicLoads	282	61.74	327.257	670.396
		2	-61.74	-327.257	-311.389
	3.Static+seismic	282	1264.539	326.967	670.086
		2	-1130.26	327.548	310.828
C856	1. Dead+Live	113	367.718	-13.475	-18.875
		141	-359.078	13.475	-21.55
	2.Seismic Loads	113	539.066	150.743	218.587
		141	-539.066	-150.743	-233.884
	3.Static+seismic	113	906.784	137.268	199.712
		141	179.987	164.218	212.334
C857	1. Dead+Live	114	585.068	-3.833	-5.408
		142	-576.428	3.833	-6.092
	2.Seismic Loads	114	59.112	256.859	371.82
		142	-59.112	-256.859	-398.976
	3.Static+seismic	114	644.179	253.025	366.274
		142	-517.316	260.692	392.884
C889	1. Dead+Live	197	138.964	-10.916	-15.557
		225	-132.484	10.916	-17.192
	2.Seismic Loads	197	90.577	74.298	103.16
		225	-90.577	-74.298	-119.756
	3.Static+seismic	197	229.542	63.381	87.602
		225	-41.907	85.214	102.564
C890	1. Dead+Live	198	236.329	-3.157	-4.533
		226	-229.849	3.157	-4.936
	2.Seismic Loads	198	31.443	115.558	165.507
		226	-31.443	-115.558	-181.171
	3.Static+seismic	198	267.772	112.401	160.974
		226	-198.406	118.714	176.234

Table 5: Beam End Forces of the Studied Frame

<i>Beam</i>	<i>L/C</i>	<i>Node</i>	<i>F_x</i> (kN)	<i>F_y</i> (kN)	<i>M_z</i> (kN.m)
B805	1. Dead+Live	1	-3.018	46.253	30.11
		2	3.018	45.267	-28.137
	2.SeismicLoads	1	25.915	215.724	447.954
		2	-25.915	-215.724	-414.941
	3.Static+seismic	1	22.897	261.977	478.064
		2	28.933	260.99	386.804
B806	1. Dead+Live	2	-2.641	45.76	30.41
		3	2.641	45.76	-30.41
	2.SeismicLoads	2	0	200.568	401.136

B807	3.Static+seismic	3	0	-200.568	-401.136
		2	-2.641	246.328	431.546
		3	2.641	246.328	370.726
	1. Dead+Live	3	-3.018	45.267	28.137
		4	3.018	46.253	-30.11
	2.SeismicLoads	3	25.915	215.724	414.941
4		-25.915	-215.724	-447.954	
3.Static+seismic	3	22.897	260.99	443.078	
	4	28.933	261.977	417.843	

Table 6: Column Stresses of the Studied Frame

<i>Column</i>	<i>L/C</i>	<i>Length</i>	<i>Max. Compressive</i>		<i>Max. Tensile</i>	
			<i>Stress (N/mm²)</i>	<i>Dist. (m)</i>	<i>Stress (N/mm²)</i>	<i>Dist. (m)</i>
C801	1. Dead+Live	3	6.355	3		
	2.SeismicLoads	3	59.056	0	-36.039	0
	3.Static+seismic	3	63.668	0	-30.671	0
C802	1. Dead+Live	3	8.42	3		
	2.SeismicLoads	3	54.063	0	-53.24	0
	3.Static+seismic	3	62.306	0	-45.445	0
C856	1. Dead+Live	3	5.977	3		
	2.SeismicLoads	3	34.229	3	-33.321	2.75
	3.Static+seismic	3	33.347	0	-32.355	2.75
C857	1. Dead+Live	3	5.768	0		
	2.SeismicLoads	3	50.521	3	-50.115	2.75
	3.Static+seismic	3	54.651	2.75	-45.852	2.75
C889	1. Dead+Live	3	5.572	3	-2.628	3
	2.SeismicLoads	3	27.97	3	-27.497	2.75
	3.Static+seismic	3	30.281	2.75	-29.002	2.75
C890	1. Dead+Live	3	3.694	0		
	2.SeismicLoads	3	40.805	3	-40.456	2.75
	3.Static+seismic	3	43.34	2.75	-38.802	2.75

Table 7: Beam Stresses of the Studied Frame

<i>Column</i>	<i>L/C</i>	<i>Length</i>	<i>Max. Compressive</i>		<i>Max. Tensile</i>	
			<i>Stress (N/mm²)</i>	<i>Dist. (m)</i>	<i>Stress (N/mm²)</i>	<i>Dist. (m)</i>
C805	1. Dead+Live	4	3.747	0	-3.798	0
	2.SeismicLoads	4	56.265	0	-55.833	0
	3.Static+seismic	4	59.995	0	-59.614	0
C806	1. Dead+Live	4	3.78	0	-3.824	0
	2.SeismicLoads	4	50.176	0	-50.176	0
	3.Static+seismic	4	53.955	0	-53.999	0
C857	1. Dead+Live	4	3.747	4	-3.798	4
	2.SeismicLoads	4	56.265	4	-55.881	3.667
	3.Static+seismic	4	57.484	3.667	-57.894	3.667

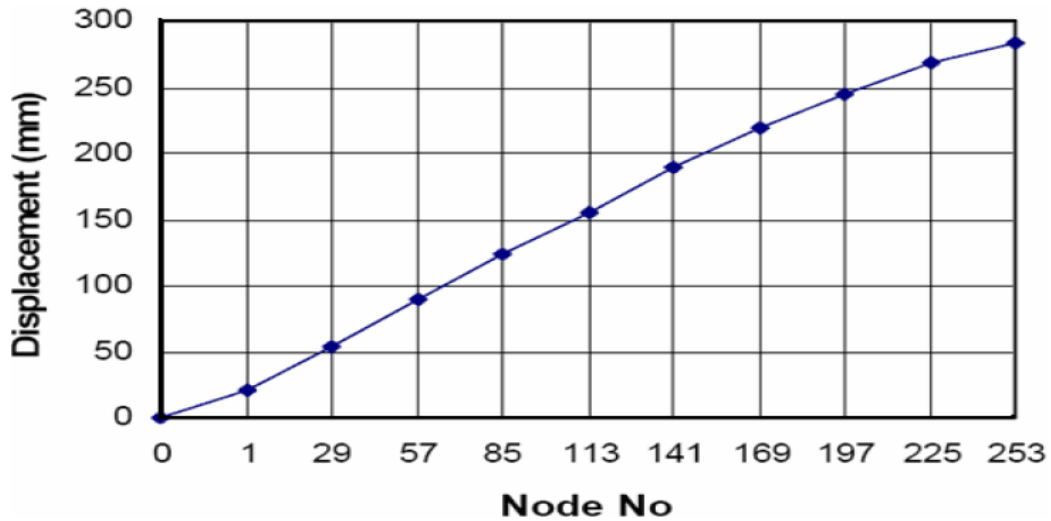


Fig. 3: Nodal Displacements of the Studied frame

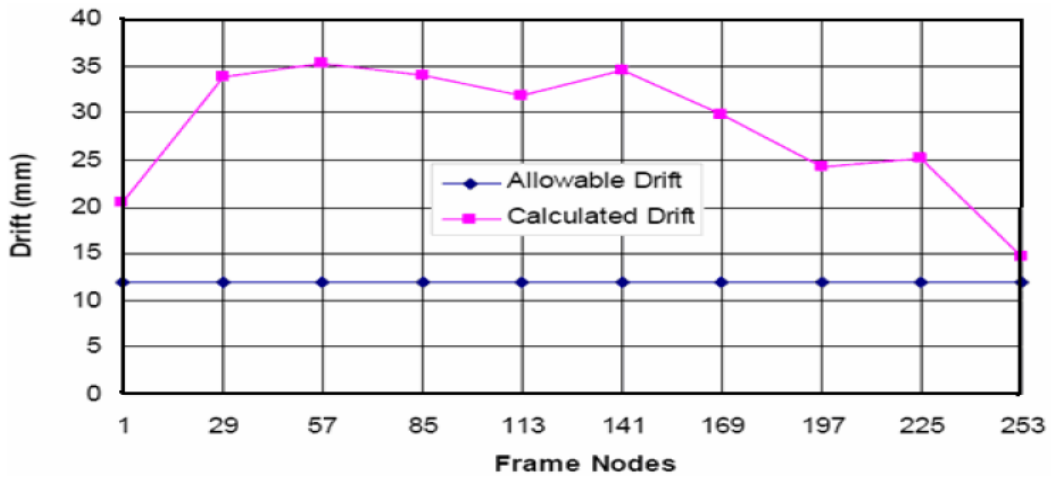


Fig. 4: Comparison between Allowable Drift and Calculated Drift of the Studied Frame

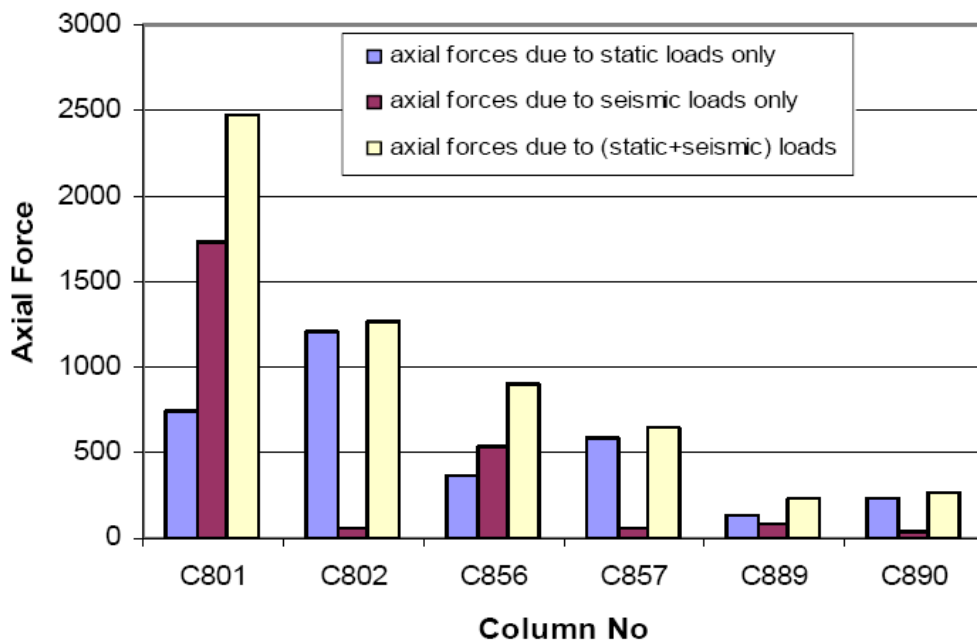


Fig. 5: Column Axial Forces of the Studied Frame

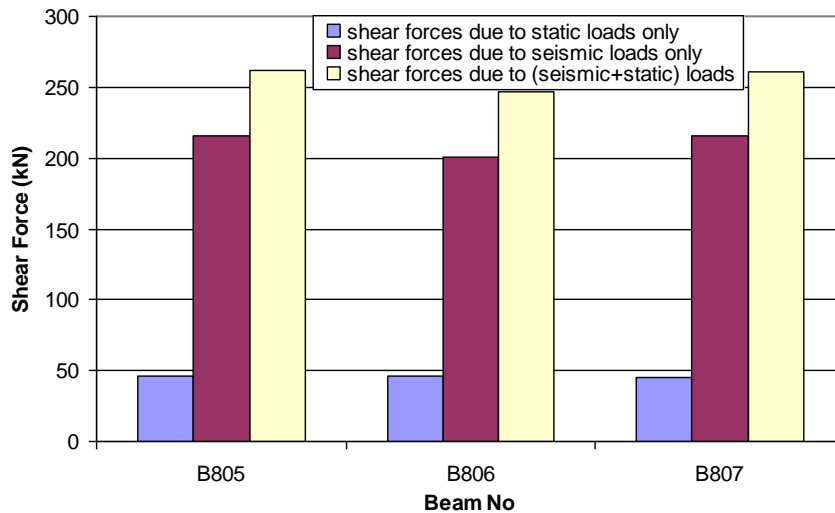


Fig. 6: Beam Shear Forces of the Studied Frame

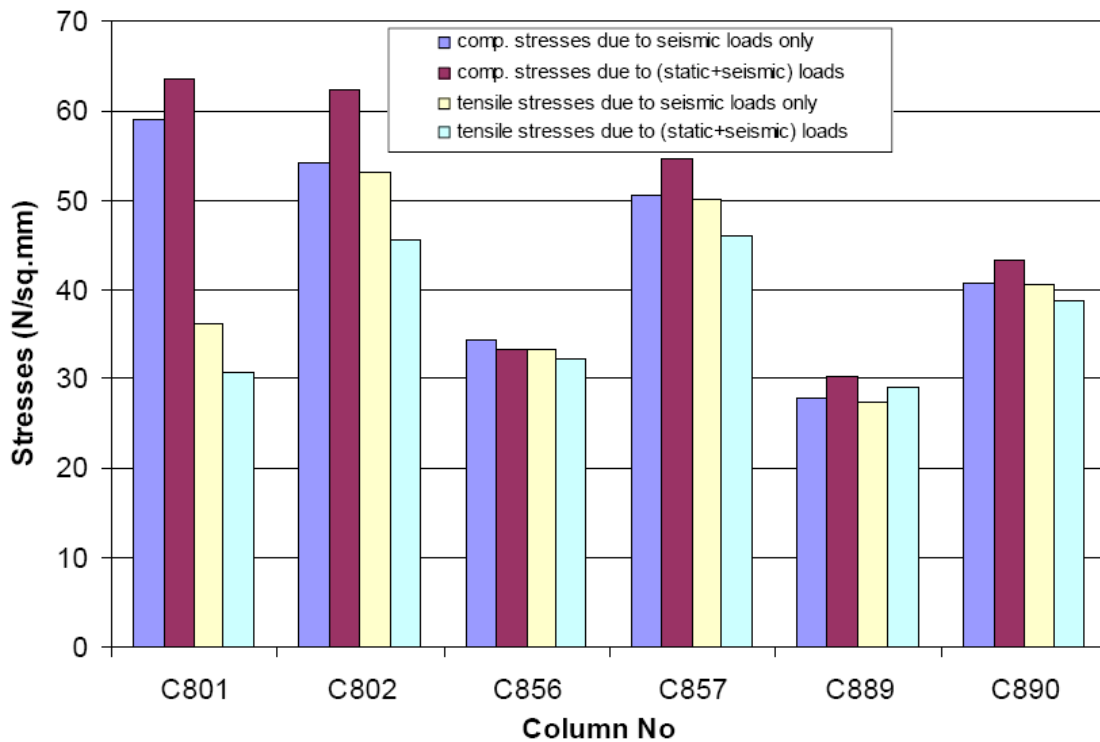


Fig. 7: Column stresses of the Studied Frame

VII. DISCUSSIONS OF THE ANALYSIS RESULTS

The results of the analysis indicated that the frame suffered a maximum horizontal displacement of 28.39 cm at its top level as shown in Table 2 and graphically in Fig. 3. This represents about 0.94% of the frame total height. These nodal displacements caused drifts in excess of the allowable drifts. Table 3 shows that the drift reached up to 35 mm in some levels while the allowable drift in this frame should not be greater than 0.004 times the story height (12 mm) []. In other words, the calculated drifts of the frame were about 2 to 3 times the allowable drifts as shown graphically in Fig. 4.

Axial forces, shear forces and bending moments increased in columns and beams due to seismic excitation. It can be observed that the axial force due to L/C3 increased in the exterior column C801 while the interior column C802 had an opposite variation trend, its axial forces due to L/C1 is greater than that of C801, whereas its axial force due to L/C3 is lesser than that of C801. However, the forces in upper floor columns showed lesser values as shown in Table 4 and Fig. 5. These values indicated that horizontal motion has a greater

effect on the axial compression loads of the exterior columns compared to the interior columns because of the overturning moment effect.

Shear forces due to the combined effect of static and seismic loads in interior columns are greater than those in exterior columns and decreased in the upper levels as in Table 4. The values of shear forces due to L/C3 in beams B805, B806 and B807 were found to be about four times the values due to L/C1 as in Table 5 and Fig. 6. These large increases of compression and shear forces can lead to compression shear failure especially if accompanied with poor detailing [7].

Table 6 and Fig.7 show that seismic excitations caused maximum compressive stresses at the bottom of C801 and C802. In other columns, these stresses occurred at different distances along the columns. It is also observed that there were no tensile stresses displayed due to L/C1. Tensile stresses in C801 and C802, generated by seismic excitation, occurred at their bottom levels. In general, compressive stresses in columns showed greater values than tensile stresses. Table 7 shows that the maximum values of compressive and tensile stresses in beams are approximately equal. These stresses mainly occurred at the end of the beams.

VIII. CONCLUSIONS

Based on the obtained results from the analysis of the reinforced concrete frame building in Khartoum city, it can be concluded that:

1. The interior columns in all floor levels were the most affected by the compression forces resulting from all cases of load combinations.
2. Bending moments in beams and columns due to seismic excitation showed much larger values compared to that due to static loads.
3. The compressive stresses generated from all cases of loads in ground floor columns were greater than tensile stresses in these columns whereas in other levels the difference was slight. The compressive stresses in ground floor columns were about 1.2 to 2 times the tensile stresses.
4. Compressive and tensile stresses in the studied beams were approximately equal.
5. The calculated drifts resulting from the nodal displacements due to the combination of static and seismic loads were about 2 to 3 times the allowable drifts.
6. The frame was inadequate to resist the applied seismic load.

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